## STRESS DISTRIBUTION IN A SLIP TRACE OF DEFORMED Ni<sub>3</sub>Ge SINGLE CRYSTALS

## Yu. A. Abzaev and V. A. Starenchenko

UDC 539.4.015

The shear-stress distribution produced by distortion of Ni<sub>3</sub>Ge single crystals under compression is studied. The evolution of the dislocation structure during deformation of Ni<sub>3</sub>Ge single crystals of various orientations ([234], [111], [139], and [001]) at T = 77, 293, 523, 673, and 873 K is analyzed. It was found that, up to failure strains, the dislocation structure is characterized by a uniform dislocation distribution. Regardless of the strain-axis orientation, the linear relation  $\tau = f(\rho^{0.5})$  is valid for all the test temperatures except for T = 77 K. The deviation from the linear relation at T = 77 K is due to the suppressed thermally activated slip of dislocations in nonuniform-strain fragments at the specimen edges. In these fragments, the shear stresses are substantially reduced, and hence, the stresses produced by the dislocation cluster retard the development of slip in this trace.

Key words: dislocation cluster, single crystal, shear strain, shear stress.

In Ni<sub>3</sub>Ge single crystals deformed under compression, strain-fragmentation regions are formed as a result of specimen distortion during shear [1, 2]. The effect of distortion of specimens under compression on the distribution of applied shear stresses has not yet been studied, and their role in the interdislocation interaction is not understood.

The goal of this work is to study the effect of distortion of a specimen under compression and stresses caused by fragmentation at the specimen edge on the shear-stress distribution along slip traces.

We studied the evolution of the dislocation structure (DS) during deformation of Ni<sub>3</sub>Ge single crystals of various orientations ([ $\overline{2}34$ ], [ $\overline{1}11$ ], [ $\overline{1}39$ ], and [001]) at test temperatures T = 77, 293, 523, 673, and 873 K. In [3–10], it was found that the DS is characterized by a uniform dislocation distribution up to failure strains. Figure 1 shows the shear stresses  $\tau$  versus the dislocation density  $\rho$  for all the orientations and test temperatures considered. One can see that the linear relation

$$\tau = \tau_F + \alpha G b \rho^{0.5} \tag{1}$$

holds for all values of T except for T = 77 K. Here  $\tau_F$  is the stress of dislocation self-retardation,  $\alpha$  is the parameter of interdislocation interaction, b is the magnitude of the Burgers vector of dislocations, and G is the shear modulus. As the temperature increases, the slope of the straight lines  $\tau = f(\rho^{0.5})$  decreases. The temperature also affects the stress  $\tau_F$ . Formula (1) approximates experimental data, which shows that the contact interdislocation interaction plays a dominant role in hardening of Ni<sub>3</sub>Ge single crystals [11–23]. The conventional strain  $\varepsilon_{\text{conv}}$ , the contributions of the reactions  $\tau_1$  and stoppers of arbitrary types  $\tau_2$  to deformation resistance, the long-range stresses  $\sigma_1$  caused by adjacent dislocations, the noncompensated fields  $\sigma_2$ , the stresses of dislocation self-retardation  $\tau_F$ , and the shear stresses  $\tau_{\text{sh}}$  for various test temperatures are listed in Tables 1–3 for the orientations [ $\overline{111}$ ], [ $\overline{139}$ ], and [ $\overline{234}$ ], respectively. The method for calculating these quantities for Ni<sub>3</sub>Ge single crystals in the [001] orientation is described in [3]. The data that allow one to determine the confidence intervals with a significance level of 99% for reactions  $\mu_1$ and those for stoppers of arbitrary types  $\mu_2$  are also given in Tables 1–3. The confidence interval of contributions of reactions and stoppers is determined by the formulas  $\tau_1 \pm \mu_1$  and  $\tau_2 \pm \mu_2$ , respectively. The dominant role in producing shear stresses is played by contact retardation of dislocations. We consider the additive contribution of various mechanisms of dislocation retardation. The contribution of stoppers of arbitrary types is much higher

Tomsk State Academy of Architecture and Construction Engineering, Tomsk 634003. Translated from Prikladnaya Mekhanika i Tekhnicheskaya Fizika, Vol. 44, No. 1, pp. 137–147, January–February, 2003. Original article submitted October 1, 2001; revision submitted April 25, 2002.



than that of long-range stresses. The contribution of stoppers of arbitrary types is mainly due to reactions. The main part of shear stresses is composed of noncompensated long-range stresses and self-retardation of dislocations. The long-range fields produced by adjacent dislocations are negligible. It was found that the effect of deformation-resistance mechanisms varies with an increase in the test temperature. In the neighborhood of peak anomalous flow stresses, superposition of individual contributions is smaller than shear stresses. This can be explained by an increasing role of virtual rectilinear barriers [7, 8, 10]. However, the main contribution to deformation resistance is made by mechanisms of contact retardation of dislocations. An analysis of Tables 1–3 shows that shear stresses are determined by mechanisms whose action is proportional to the linear density of stoppers at the dislocation line. Elastic stress fields of dipoles, which can lead to deviation from relation (1), are insignificant part of shear stresses and decrease as strains increase [3]. The relation  $\tau = f(\rho^{0.5})$  is nonlinear for all the orientations studied at T = 77 K (Fig. 1). An analysis of the slip-band pattern on the surface shows that rough slip occurs at T = 77 K. Similar results were obtained in [24]. At T = 77 K, thermally activated motion of dislocations is suppressed. Dislocations are appreciably attached to their slip plane. Slip fragmentation caused by distortion of single crystals with increasing strain shows that the external-stress distribution along the slip traces at the specimen edges is nonuniform [1, 2].

We consider the shear-stress distribution along the slip trace LPDF (Fig. 2). Upon leaving the region of uniform strain at the point D, the dislocations in the slip plane continue to move as shear stresses decrease. They cease to move upon attaining a point in the trace at which the external stress approaches the yield point (point T in Fig. 2b). In the local volume considered, the shear stresses act on the upper surface only (Fig. 2a). On the lower surface, the stresses vanish along the strain axis. As a result, the trace of the slip system passes from the line DE

ΤA	BL	Æ	1
----	----	---	---

		1	1						
T, K	$\varepsilon_{\rm conv}, \%$	$\tau_1$ , MPa	$\tau_2$ , MPa	$\sigma_1$ , MPa	$\sigma_2$ , MPa	$\mu_1$ , MPa	$\mu_2$ , MPa	$\tau_{\rm sh},{\rm MPa}$	$\tau_F$ , MPa
77	$5.57 \\ 10.13 \\ 19.5$	22.3 12.9 28.2	$74.3 \\ 69.0 \\ 75.6$	$12.2 \\ 10.2 \\ 14.4$	$39.6 \\ 43.0 \\ 36.2$	$10.3 \\ 7.8 \\ 9.2$	$20.7 \\ 21.2 \\ 14.9$	$58.9 \\ 80.4 \\ 165.8$	20
293	$5 \\ 10 \\ 16$	$\begin{array}{c} 49.7 \\ 84.6 \\ 55.6 \end{array}$	190 198 229	$37.4 \\ 56.8 \\ 51.5$	79.3 98.1 121.0	$24.0 \\ 36.3 \\ 30.2$	$32.7 \\ 40.0 \\ 46.9$	$168.1 \\ 312.0 \\ 328.0$	48.5
523	5 10 16 21	60.1 48.0 103.0 110.0	148 119 223 286	$23.0 \\ 22.2 \\ 62.5 \\ 69.4$	74.6 77.7 113.0 142.0	14.7 13.4 40.0 40.8	30.6 31.2 44.4 53.7	$239.1 \\ 295.1 \\ 352.2 \\ 150.6$	3.8
673	10 15 21	82.6 94.1 119.0	175 226 253	39.7 39.2 48.6	81.5 132.0 132.0	24.7 25.1 31.1	$32.7 \\ 53.6 \\ 41.0$	$264.1 \\ 340.8 \\ 472.0$	20
873	5 11 18 30	24.6 39.5 48.3 53.3	101 112 110 138	$     11.4 \\     24.2 \\     18.4 \\     32.4   $	43.7 57.9 66.1 82.7	$7.1 \\ 15.0 \\ 11.4 \\ 27.6$	17.7 23.8 27.6 34.5	$156.5 \\ 153.3 \\ 221.0 \\ 212.3$	47

TABLE 2

T, K	$\varepsilon_{\rm conv}, \%$	$\tau_1$ , MPa	$\tau_2$ , MPa	$\sigma_1$ , MPa	$\sigma_2$ , MPa	$\mu_1$ , MPa	$\mu_2$ , MPa	$\tau_{\rm sh},{\rm MPa}$	$\tau_F$ , MPa
77	5 10 18	30 38 76	72 92 148	$13 \\ 16 \\ 35$	27 28 68	8 4 21	11 11 20	$71.0 \\ 154.4 \\ 250.0$	20
293	$2.8 \\ 5 \\ 7.8 \\ 11$	120 150 170 190	280 260 300 370	$44 \\ 43 \\ 46 \\ 54$	95 73 88 110	28 26 27 32	41 29 35 36	564.2 696.2 911.6 1064.2	100
523	$2.45 \\ 6.8 \\ 9$	73 82 91	150 190 200	49 32 43	55 59 75	15 19 25	$22 \\ 24 \\ 30$	585.9 703.1 732.3	348
673	$2.3 \\ 6.4 \\ 8.45$	$\begin{array}{c} 42\\68\\84\end{array}$	100 210 200	21 36 31	41 89 80	13 21 19	16 36 32	322.9 398.6 448.6	167
873	$     4.8 \\     7.24 \\     12.6 $	39 38 45	83 88 120	24 21 21	$38 \\ 36 \\ 61$	13 12 12	$     15 \\     14 \\     23   $	186.2 177.8 183.4	74





1 1

Ť

τ

Î

1 1

Î

1 1

to the line DF (Fig. 2a). Figure 2b shows the considered region DEF. Obviously, the slope of the line DE is determined by accumulated shear power DF. By virtue of uniformity, the shear stresses at different points of the trace PD in the region ABKV (Fig. 2a) are identical and coincide with applied external stresses.

We now consider the shear-stress distribution along the trace DF. The final configuration of the region DEF (Fig. 2a) can be assumed to result from the following displacements. Under the action of stresses, the point N (Fig. 2b) is shifted to the point D. At the point F, the applied stresses vanish. To determine strains at the point T at the line DF, we use the finite-element method [26]. The coordinates of the points D, T, and F at the line DF are related by the equation

$$\frac{y_T - y_F}{y_D - y_F} = \frac{x_T - x_F}{x_D - x_F} \quad \text{or} \quad y_T = \frac{y_D}{x_D} x_T.$$
(2)

117



Dividing Eq. (2) by  $l_0$  (initial length of the specimen), we obtain the following relation between the relative displacements  $u_D$  and  $u_T$  at the points D and T:

$$u_T = (u_D/x_D)x_T, \qquad u_T = (x_T/x_D)u_D.$$
 (3)

We consider the triangle DMF. Using the sine theorem, we obtain

$$|DF|/\cos\beta = |DM|/\cos\left(\alpha + \beta\right),\tag{4}$$

where  $x_D = |DM|$  and  $\beta$  is the slope angle of the slip plane. Before deformation, we have |DF| = |DE|. Under compression along the line ND, the line DF is stretched. Provided the strain volume remains unchanged, the variation in the cross-sectional area is given by  $S_{\varepsilon} = S_0 \exp(+\varepsilon)$ , whence  $|DF| \approx |DE| \exp(+\varepsilon/2)$  (the plus denotes extension). For nonuniform strains at the line DF, this relation is approximate. Substituting the values of |DF|and |DM| into formulas (3) and (4), respectively, we obtain

$$\frac{x_T}{DE|} = \frac{\cos\left(\alpha + \beta\right)}{\cos\beta} \exp\left(+\frac{\varepsilon}{2}\right) \frac{\varepsilon_T}{\varepsilon_D}.$$
(5)

We write Eq. (5) in terms of stresses. To this end, we assume that the relative displacements at the points N and T (Fig. 2b) occur in the region of elastic strains of the crystal lattice and, hence, they are proportional to stresses:

$$\frac{x_T}{|DE|} = \frac{\cos\left(\alpha + \beta\right)}{\cos\beta} \exp\left(+\frac{\varepsilon}{2}\right) \frac{\tau_T}{\tau_D}.$$
(6)

If the current stress at the point T is equal to the yield point, i.e.,  $\tau_T = \tau_{0.2}$ , one can use formula (6) to estimate the yield-point distribution along the trace DF. The external stresses along the line DF decrease from maximum values at the point D equal to applied external stresses to minimum values at the point F.

In this case,  $x_{0.2}/|DE|$  in (6) is the relative magnitude of the trace DF; at the segment DT of this trace, external stresses decrease to the yield point. The slope of the trace at the specimen edge was determined experimentally for different levels of strain. For the [ $\overline{2}34$ ] orientation, it was found that  $\alpha = 1, 2, 3, 5$ , and 8° and  $\sigma_D = 68.8, 99.0, 164.1, 273.7, and 427.0$  MPa for the strain  $\varepsilon = 4, 8, 15, 20, and 24\%$ , respectively. The yield point is  $\tau_{0.2} = 46.9$  MPa. The calculation results are shown in Fig. 3. Along the line DF, the flow stresses decrease abruptly from  $\sigma = 427$  MPa at the point D to the yield point at a distance of approximately 0.1|DF|. This means that stresses acting on the remaining part of DF are too low to cause shear strain. Deformation in the shear zone can be caused only by long-range stresses of dislocations newly formed in a cluster, which shift previously formed dislocations toward the crystal surface. In this case, the stress fields are strongly nonuniform. The specific feature of this mechanism is that movable dislocations (see Fig. 2c) and the dislocation cluster 1–4 lie in the same slip plane, and shear along the trace TF is difficult to occur. It is likely that the revealed mechanism of slip termination is most pronounced at low temperatures (T = 77 K), since thermally activated processes are difficult to develop in this case. Dislocations are strongly attached to the shear zone, and, as a result, the long-range stresses must increase to shift the dislocations in the cluster to the specimen surface. The relative displacements of the points N and T (see Fig. 2b) due to deformation can be expressed in terms of the conventional strain of the specimen  $\varepsilon_{\text{conv}}$  at these points. Indeed, the strain at the point N is given by  $(l_N - l_0)/l_0 = (l_0 - |ND| - l_0)/l_0 = -|ND|/l_0 = \varepsilon_{\text{conv}}$  and that at the point T is  $(l_0 - y_T - l_0)/l_0 = -y_T/l_0 = \varepsilon_{\text{conv}}$  (the minus denotes compression). The relative displacements are equal to the conventional strains of the specimen at the points N and T.

The true strain  $\varepsilon$  and the conventional strain  $\varepsilon_{\text{conv}}$  are related by the formula  $\varepsilon = \ln (1 + \varepsilon_{\text{conv}})$  and differ only slightly for strains varied within 20%.

We use the finite-element method assuming that the line DF remains straight. The physical basis of this assumption is as follows. Rotation of the line DF corresponds to the plane problem. We calculate the ratio of the increments  $u_T/\Delta x$  of the point T on the line DF ( $u_T$  is the displacement along the strain axis and  $\Delta x$  is the displacement in the perpendicular direction). For small angles  $\alpha$ , this ratio is proportional to  $\tan \alpha$  [27]. For a constant strain volume, we have

$$\frac{u_T}{\Delta x} \approx \frac{l_0 \exp\left(-\varepsilon\right) - l_0}{S_0^{0.5} \exp\left(+\varepsilon/2\right) - S_0^{0.5}}$$

Passing to the limit as  $\Delta x \to 0$ , we obtain

$$l_0 \frac{d\varepsilon_{\rm conv}}{dx} = l_0 \frac{\exp\left(-\varepsilon\right) - 1}{S_0^{0.5}(\exp\left(+\varepsilon/2\right) - 1)}, \qquad \frac{d\varepsilon_{\rm conv}}{dx} = C \frac{\exp\left(-\varepsilon\right) - 1}{\exp\left(+\varepsilon/2\right) - 1},\tag{7}$$

where C = const and  $S_0$  is the initial cross-sectional area of the specimen. Using the above-mentioned relation between the true and conventional strains, we write the solution of Eq. (7) in the form

 $2\exp\left(+3\varepsilon/2\right)3\exp\left(+\varepsilon\right) + 6\exp\left(+\varepsilon/2\right) - 6\ln\left(1 + \exp\left(+\varepsilon/2\right)\right) = -3Cx + D,\tag{8}$ 

where D = const. Expanding the left side in (8) into a power series, we obtain

$$(5 - 6 \ln 2) + 1.5\varepsilon + (57/16)\varepsilon^2 + \ldots = -3Cx + D.$$

For  $\varepsilon = 19\%$ , the quadratic term in the solution is smaller than the linear term by almost a factor of 3. Therefore, it can be assumed that the linear relation  $\varepsilon = f(x)$  is valid, i.e., approximation of DF by a straight line in the finite-element method is physically justified. Retaining quadratic terms in (8), we obtain the parabolic relation  $\varepsilon^2 = f(x)$ .

Let us estimate the possible contribution of the reversed stress caused by dislocations accumulated at the specimen edge to deformation resistance and also the deviation from relation (1). A cluster of dislocations is formed along the slip trace DF (see Fig. 2b and c). In the tail of the cluster, the shear stresses approach the yield point. It is assumed that dislocations cannot slide at these stresses. The first dislocation ceases to move near the point T. The second dislocation that follows the first one (it also ceases to move near the point T) shifts the first dislocation along the trace at a distance where the sum of stresses of interaction between these dislocations and the external stress that acts on the first dislocation (this sum is smaller than the yield point, which is taken into account by the coefficient  $\gamma$ ) becomes equal to the yield point. We write the condition of equilibrium for the first dislocation:

$$\gamma \tau_0 + Gb/(2\pi K x_1) \approx \tau_0. \tag{9}$$

Here  $x_1$  is the distance between the first and second dislocations,  $\tau_0$  is the yield point,  $\gamma\tau_0$  is the stress acting on the first dislocation, and  $K = 1 - \nu$  ( $\nu$  is Poisson's ratio). We estimate the distance  $x_1$  at which the first dislocation is shifted toward *DF*. Obviously, the quantity  $\gamma$  is indeterminate. We assume that the first dislocation passed a distance such that the applied stresses decrease to 0.9 of the yield point ( $\gamma = 0.9$ ). Consequently, Eq. (9) can be written in the form

$$Gb/(2\pi Kx_1) \approx 0.1\tau_0. \tag{10}$$

We calculate the distance  $x_1$  for the [111] orientation. The shear modulus G is taken to be  $8 \cdot 10^4$  MPa,  $\nu = 1/3$ , b = 0.25 nm, and the yield point is  $\tau_0 \approx 55$  MPa. Substitution of these values into formula (10) yields  $x_1 \approx 870$  nm. We consider the formation of the dislocation cluster in the slip trace DF and estimate the number of dislocations for the strain  $\varepsilon \approx 19.5\%$ . In this case, the shear stresses are  $\tau \approx 165$  MPa. We write the equation of equilibrium of the *n*th dislocation near the point T (see Fig. 2c):

$$Gb/(2\pi Kx_1)(1+1/2+1/3+1/4+\ldots+1/n) \approx \tau.$$
 (11)

119

In formula (11), the following approximation is used. The dislocations in the cluster are distributed uniformly and the distance between them is equal to  $x_1$ . The bracketed numerical series is divergent. We find a partial sum of the series. For a sufficiently large number of terms, we have [17, 25]

$$S_n = 1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \ldots + \frac{1}{n} \approx \int_{1}^{n} \frac{dn}{n} = \ln n.$$
(12)

More accurate estimates of the partial sum given in [25] show that  $S_n \approx \ln n + 5.6$ . Substituting the partial sum  $S_n$  from formula (12) into formula (11) and assuming that the applied stresses are equal to  $\tau \approx 165$  MPa, we obtain the number of dislocations n in the cluster:

Ln 
$$n \approx 2\pi (1 - \nu) x_1 \tau / (Gb) - 5.6$$
.

For the parameters chosen, this formula yields  $n \approx \exp(24.4) \approx 4 \cdot 10^{10}$ . Obviously, this number of dislocations in the cluster DF is overestimated. Most of these dislocations arrive at the surface and form a rough trace. We estimate the possible number of dislocations, in the trace DF, that can be held by the first dislocation in the cluster. To this end, it is necessary to write the equation of equilibrium of the first dislocation (see Fig. 2c). This dislocation can retard the motion of n-1 subsequent dislocations in the cluster if superposition of paired interactions of all dislocations with applied stresses does not exceed the yield point for the first dislocation. Since the parameter  $\gamma$ is indeterminate, the calculations are approximate. Setting  $\gamma = 0.1$ , we obtain  $\tau \approx \gamma \tau_0 = 0.1 \tau_0$ . The equation of equilibrium (11) becomes

$$0.1\tau_0 + Gb/(2\pi Kx_1)(1 + 1/2 + 1/3 + 1/4 + \ldots + 1/n) \approx \tau_0.$$

Simple calculations yield  $\operatorname{Ln} n \approx 9 - 5.6 = 3.4$ . It follows that, for  $\varepsilon = 19.5\%$  and T = 77 K, the number of dislocations in the cluster is  $n \approx 30$ . It is worth noting that the equidistant dislocation distribution in the cluster determines the lower boundary of the number of dislocations. Dislocations in the cluster DF are responsible for deviation from the linear relation  $\tau = f(\rho^{0.5})$ . Since the number of dislocations in the cluster depends on the dislocation density  $\rho$ , the contribution to deformation resistance at T = 77 K should be higher than that predicted by the linear relation  $\tau = f(\rho^{0.5})$ . We determine the contribution to deformation resistance using the Seeger formula [23]. This formula allows one to calculate the long-range stresses caused by clusters of dislocations at distances comparable with the average distance between dislocations:

$$\tau = Gb\sqrt{n}\rho^{1/2}/(2\pi K).$$

For  $\varepsilon = 19.5\%$ , we have  $\rho \approx 10.4 \cdot 10^9 \text{ cm}^{-1}$ . The other parameters are listed above. The estimates show that  $\tau \approx 266.9$  MPa. The contribution of clusters at the specimen edge to deformation resistance is rather considerable, compared to that of shear stresses. The stress calculated by the formula

$$\tau = Gb\rho^{1/2} \operatorname{Ln} n/(2\pi K),$$

which takes into account the stresses caused by clusters of dislocations, is equal to 165 MPa. An analysis of the number of dislocations in the cluster DF for other orientations shows that  $n \approx 30$  for all the orientations. Even for the [ $\overline{1}39$ ] orientation, for which the yield point is approximately 1.5 times that for the [ $\overline{1}11$ ] orientation, this number is close to  $n \approx 30$ . An analysis of the image stresses  $\tau_{\rm im}$  that occur owing to the effect of the specimen surface and act on the head dislocation shows that they are negligible [17]:  $\tau_{\rm im} = Gb/(4\pi(L_{\rm surf} - L_{\rm cluster})) \approx 1/6300$  MPa, where  $L_{\rm surf}$  is the distance from the surface to the head dislocation and  $L_{\rm cluster}$  is the length of the cluster ( $L_{\rm surf} \approx 10^{-4}$  m and  $L_{\rm cluster} \approx 2700$  nm for T = 77 K and  $\varepsilon \approx 20\%$ ).

Thus, it has been shown that the contributions of dislocation clusters in the slip plane at the specimen edge to deformation resistance can have a considerable effect on flow stresses at low test temperatures (T = 77 K), which results in deviation from the linear relation  $\tau = f(\rho^{0.5})$ . The deviation from the linear relation is due to the fact that sliding dislocations are attached to their slip plane owing to weak thermally activated processes on dislocations.

## REFERENCES

- Yu. A. Abzaev, Yu. V. Solov'eva, É. V. Kozlov, et al., "Calculation of shear stresses in single crystals of the Ni<sub>3</sub>Ge alloy," *Izv. Vyssh. Uchebn. Zaved., Fiz.*, No. 6, 48–53 (1995).
- Yu. A. Abzaev, V. A. Starenchenko, Yu. V. Solov'eva, et al., "Analysis of fragmentation of deformation in Ni<sub>3</sub>Ge single crystals," J. Appl. Mech. Tech. Phys., **39**, No. 1, 135–139 (1998).
- Yu. A. Abzaev, V. A. Starenchenko, N. A. Koneva, and É. V. Kozlov, "Evolution of the dislocation structure and hardening mechanisms of Ni<sub>3</sub>Ge single crystals oriented for multiple slip," *Izv. Vyssh. Uchebn. Zaved., Fiz.*, No. 3, 65–70 (1987).
- V. A. Starenchenko, Yu. A. Abzaev, and N. A. Koneva, "Stability loss of uniform plastic strain of Ni<sub>3</sub>Ge single crystals," *Fiz. Met. Metalloved.*, 64, No. 6, 1178–1182 (1987).
- V. A. Starenchenko, Yu. A. Abzaev, N. A. Koneva, and É. V. Kozlov, "Thermal hardening and evolution of the dislocation structure of Ni<sub>3</sub>Ge single crystals," *Fiz. Met. Metalloved.*, 68, No. 3, 595–601 (1989).
- 6. V. A. Starenchenko and Yu. A. Abzaev, "Temperature dependence of parameters of interdislocation interaction in Ni<sub>3</sub>Ge single crystals," *Metallofizika*, No. 2, 131–136 (1991).
- V. A. Starenchenko, Yu. A. Abzaev, Yu. V. Solov'eva, and É. V. Kozlov, "Thermal hardening of Ni<sub>3</sub>Ge single crystals," *Fiz. Met. Metalloved.*, **79**, No. 1, 147–155 (1995).
- 8. V. A. Starenchenko, Yu. V. Solov'eva, Yu. A. Abzaev, and B. I. Smirnov, "Orientation dependence of thermal hardening of single crystals of the Ni<sub>3</sub>Ge alloy," *Fiz. Tverd. Tela*, No. 38, 3050–3058 (1996).
- 9. V. A. Starenchenko, Yu. V. Solov'eva, Yu. A. Abzaev, et al., "Evolution of the dislocation structure during deformation of Ni<sub>3</sub>Ge single crystals of various orientations," *Fiz. Tverd. Tela*, **40**, No. 4, 81–89 (1998).
- 10. V. A. Starenchenko, Yu. V. Solov'eva, and Yu. A. Abzaev, "Accumulation of dislocations and thermal hardening in alloys with an L1<sub>2</sub> superstructure," *Fiz. Tverd. Tela*, **41**, No. 3, 454–460 (1999).
- J. N. Lomer and H. M. Rozenberg, "The detection of dislocation by the temperature heat conductivity measurements," *Philos. Mag.*, 4, No. 340, 467–483 (1959).
- 12. R. W. K. Honeycombe, The Plastic Deformation of Metals, Edward Arnold, London (1968).
- 13. J. Weertman and J. Wirtman, in: R. W. Cahn (ed.), Physical Metallurgy, North-Holland, Amsterdam (1956).
- 14. L. I. Mirkin, Physical Fundamentals of Strength and Plasticity [in Russian], Izd. Mosk. Univ., Moscow (1968).
- 15. D. McLean, Mechanical Properties of Metals John Wiley and Sons, New York–London (1962).
- 16. H. G. van Bueren, Imperfections in Crystals, North-Holland, Amsterdam (1960).
- 17. J. Fridel, Dislocations, Pergamon Press, Oxford (1964).
- N. A. Koneva, L. A. Teplyakova, É. V. Kozlov, "Nature of hardening of ordered alloys with an L1<sub>2</sub> superstructure," in: *Structure and Plastic Behavior of Alloys* [in Russian], Izd. Tomsk. Univ., Tomsk (1983), pp. 74–99.
- N. A. Koneva and E. V. Kozlov, "Nature of substructural hardening," Izv. Vyssh. Uchebn. Zaved., Fiz., No. 8, 3– 14 (1982).
- N. A. Koneva and É. V. Kozlov, "Special features of substructural hardening," Izv. Vyssh. Uchebn. Zaved., Fiz., No. 3, 56–70 (1991).
- G. I. Taylor, "The mechanism of plastic deformation of crystals. Part 1. Theoretical," in: Proc. Roy. Soc. London, Ser. A, 145 (1934), pp. 362–387.
- 22. N. F. Mott, "The work hardening of metals," Trans. AIME, No. 6, 962–968 (1960).
- A. Seeger, J. Diehl, S. Mader, and H. Rebstock, "Workhardening and worksoftening of face-centered cubic metal crystals," *Philos. Mag.*, 2, No. 15, 323–350 (1957).
- H.-R. Pak, T. Saburi, and S. Nenno, "The effect on the temperature dependence of yield stress in Ni<sub>3</sub>Ge single crystals," *Trans. Jpn. Inst. Metals*, **19**, No. 1, 35–42 (1978).
- 25. A. A. Predvoditelev, "Possible ways to construct the hardening theory based on tests on dislocations," in: *Physics of Deformation Hardening of Single Crystals* [in Russian], Naukova Dumka, Kiev (1972), pp. 74–94.
- 26. L. J. Segerlind, Applied Finite Element Analysis, John Wiley and Sons, New York (1976).
- 27. L. D. Landau and E. M. Lifshitz, *Theory of Elasticity*, Pergamon Press, Oxford (1986).